## Analysis of Covariance

### Analysis of covariance

- ANOVA: explanatory variables categorical (divide data into groups)
- traditionally, analysis of covariance has categorical x's plus one numerical x ("covariate") to be adjusted for.
- 1m handles this too.
- Simple example: two treatments (drugs) (a and b), with before and after scores.
- Does knowing before score and/or treatment help to predict after score?
- Is after score different by treatment/before score?

### Data: treatment, before, after

- a 5 20
- a 10 23
- a 12 30
- a 9 25
- a 23 34
- a 21 40
- a 14 27
- a 18 38
- a 6 24
- a 13 31
- b 7 19
- b 12 26
- b 27 33
- D 21 33
- b 24 35
- b 18 30
- b 22 31
- b 26 34
- b 21 28
- b 14 23
- b 9 22

## **Packages**

```
library(tidyverse)
library(broom)
library(marginaleffects)
```

the last of these for predictions.

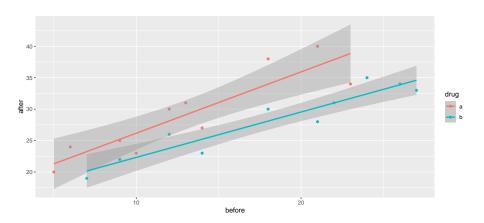
#### Read in data

```
url <- "http://ritsokiguess.site/datafiles/ancova.txt"
prepost <- read_delim(url, " ")
prepost</pre>
```

```
# A tibble: 20 x 3
   drug before after
   <chr> <dbl> <dbl>
              5
 1 a
                   20
2 a
             10 23
3 a
             12 30
4 a
                   25
 5 a
           23
                   34
6 a
             21
                   40
7 a
             14
                   27
             18
                   38
8 a
 9 a
              6
                   24
10 a
             13
                   31
```

## Making a plot

```
ggplot(prepost, aes(x = before, y = after, colour = drug)) +
geom_point() + geom_smooth(method = "lm")
```



#### Comments

- As before score goes up, after score goes up.
- Red points (drug A) generally above blue points (drug B), for comparable before score.
- Suggests before score effect and drug effect.

#### The means

```
prepost %>%
  group_by(drug) %>%
  summarize(
   before_mean = mean(before),
   after_mean = mean(after)
)
```

- Mean "after" score slightly higher for treatment A.
- Mean "before" score much higher for treatment B.
- Greater improvement on treatment A.

### Testing for interaction

```
prepost.1 <- lm(after ~ before * drug, data = prepost)</pre>
drop1(prepost.1, test = "F")
Single term deletions
Model:
after ~ before * drug
            Df Sum of Sq RSS AIC F value Pr(>F)
                         109.98 42.092
<none>
before:drug 1 12.337 122.32 42.218 1.7948 0.1991
```

• Interaction not significant. Will remove later.

### **Predictions**

Set up values to predict for, median and quartiles for before, the two drugs:

```
before drug rowid
1 9.75 a 1
2 9.75 b 2
3 14.00 a 3
4 14.00 b 4
5 21.25 a 5
6 21.25 b 6
```

#### and then

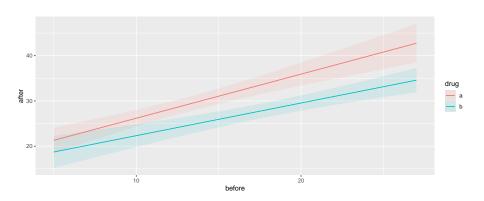
```
cbind(predictions(prepost.1, newdata = new)) %>%
  select(drug, before, estimate, conf.low, conf.high)

drug before estimate conf.low conf.high
1 a 9.75 25.93250 24.05059 27.81442
```

```
1 a 9.75 25.93250 24.05059 27.81442
2 b 9.75 22.14565 19.58681 24.70450
3 a 14.00 30.07784 28.43296 31.72271
4 b 14.00 25.21304 23.32649 27.09959
5 a 21.25 37.14929 34.32557 39.97300
6 b 21.25 30.44565 28.64373 32.24758
```

Analysis of Covariance

# Predictions (with interaction included), plotted



Lines almost parallel, but not quite.

### Taking out interaction

```
prepost.2 <- update(prepost.1, . ~ . - before:drug)
drop1(prepost.2, test = "F")</pre>
```

```
Single term deletions
```

```
Model:

after ~ before + drug

Df Sum of Sq RSS AIC F value Pr(>F)

<none> 122.32 42.218

before 1 540.18 662.50 74.006 75.074 1.211e-07 ***
drug 1 115.31 237.63 53.499 16.025 0.0009209 ***
---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

- Take out non-significant interaction.
- before and drug strongly significant.
- Do predictions again and plot them.

### **Predictions**

2

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5

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b 9.75 21.27328

a 14.00 29.94473 b 14.00 24.79007

a 21.25 35.94397

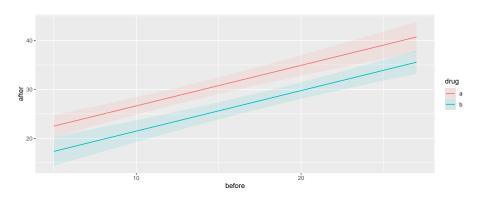
b 21,25 30,78931

```
cbind(predictions(prepost.2, newdata = new)) %>%
  select(drug, before, estimate)

drug before estimate
1   a  9.75 26.42794
```

## Plot of predicted values

plot\_predictions(prepost.2, condition = c("before", "drug"))



This time the lines are *exactly* parallel. No-interaction model forces them to have the same slope.

### Different look at model output

• drop1(prepost.2) tests for significant effect of before score and of drug, but doesn't help with interpretation.

Analysis of Covariance

• summary(prepost.2) views as regression with slopes:

```
summary(prepost.2)
```

```
Call:
lm(formula = after ~ before + drug, data = prepost)
Residuals:
   Min
            10 Median
                           30
                                  Max
-3.6348 -2.5099 -0.2038 1.8871 4.7453
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                       1.5115 12.147 8.35e-10 ***
(Intercept) 18.3600
before
         0.8275
                       0.0955 8.665 1.21e-07 ***
          -5.1547 1.2876 -4.003 0.000921 ***
drugb
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 2.682 on 17 degrees of freedom
```

Multiple R-squared: 0.817, Adjusted R-squared: 0.7955

## Understanding those slopes

#### tidy(prepost.2)

- before ordinary numerical variable; drug categorical.
- 1m uses first category druga as baseline.
- Intercept is prediction of after score for before score 0 and drug A.
- before slope is predicted change in after score when before score increases by 1 (usual slope)
- Slope for drugb is *change* in predicted after score for being on drug B rather than drug A. Same for *any* before score (no interaction).

### Summary

- ANCOVA model: fits different regression line for each group, predicting response from covariate.
- ANCOVA model with interaction between factor and covariate allows different slopes for each line.
- Sometimes those lines can cross over!
- If interaction not significant, take out. Lines then parallel.
- With parallel lines, groups have consistent effect regardless of value of covariate.

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